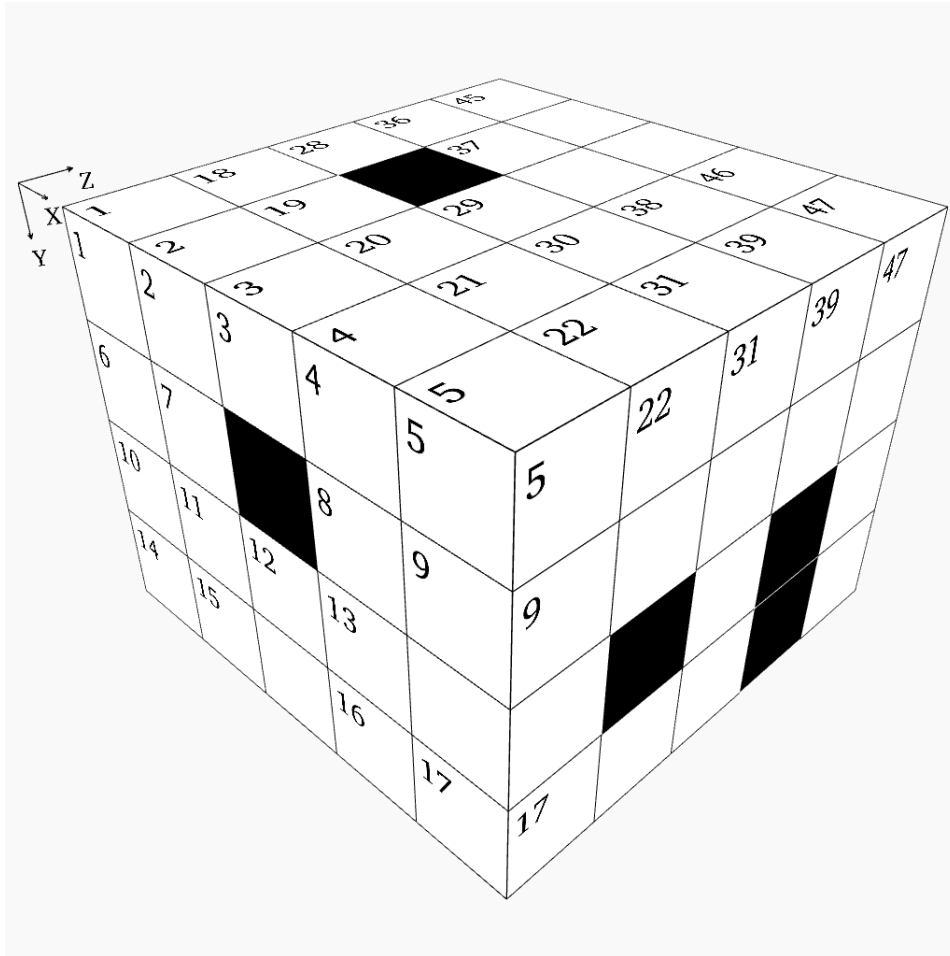


Difficulty: ★★★★★

Box - Hard Puzzle #19



This puzzle is like a crossword, but with numbers. Each digit occupies a 3D block and can be a part of a "word" in the X, Y, and Z directions.

Rules:

1. "Words" may not start with a zero.
2. "Words" in the X direction read from left to right.
3. "Words" in the Y direction read from top to bottom.
4. "Words" in the Z direction read from front to back.
5. There is one unique solution which satisfies all the clues given below.
6. Some "words" may not have clues. They will be determined by the "words" which intersect them.

If we take the box pictured above and divide it into individual X-Y layers, we will get these planes:

1	2	3	4	5	18	19	20	21	22	28		29	30	31
6	7		8	9	23		24			32	33			
10	11	12	13		25								34	
14	15		16	17	26			27		35				

36	37		38	39	45			46	47
			40					48	
41		42			49	50			
43			44		51			52	

X Direction

- 1 A prime number
- 6 $X_{40} - Y_{12}$
- 8 $Z_9 - X_4$
- 10 A prime number
- 14 Twice a prime number
- 18 Twice the result of $X_{23} + X_4$
- 23 Forty-three times a prime number
- 25 A square
- 26 Mean of X_{27} and X_{34}
- 27 $X_{35} + Z_2$
- 29 $Y_{33} - Y_{50}$
- 32 Sixteen thousand four hundred nine less than X_{14}
- 34 A square
- 35 $Z_{10} - X_{34}$
- 36 A prime number
- 40 $X_{34} + X_{26}$
- 41 Twice the result of $X_{45} - X_{36}$
- 43 Thirteen times a prime number
- 45 Two thousand eight hundred thirty more than Z_5
- 48 $Y_{42} - Z_{37}$
- 49 Seventeen times a prime number
- 51 Mean of Y_{50} and Z_{24}
- 52 $Z_2 + Y_{41}$

Y Direction

- 1 $Y_{29} \times X_{52}$
- 2 Mean of Y_{46} and X_{40}
- 4 Half of Y_5 , then subtract Y_{33}
- 5 Fourteen times a prime number
- 12 Mean of Z_{10} and Z_{16}
- 18 $X_6 + X_{41}$
- 19 Thirty-eight times a prime number
- 20 $Y_{22} + X_{51}$
- 21 One thousand three hundred seventy-six more than Y_{31}
- 22 A cube
- 28 $Y_{31} \div X_{27}$
- 29 Mean of X_8 and Z_{41}
- 30 Rearranged digits of X_{29}
- 31 $Y_{20} \times X_{26}$
- 33 $Z_{17} + X_{48}$
- 37 Mean of Y_{29} and Y_{46}
- 38 Thirty-one times a prime number
- 39 $Y_{28} - Y_{12}$
- 41 Mean of X_{51} and X_{26}
- 42 $Z_{44} - \text{half of } Y_{12}$
- 45 A square
- 46 Twice a square
- 47 $X_{51} + Y_{37}$
- 50 $X_6 + Z_{16}$

Z Direction

- 1 One thousand eight hundred nine less than Z_9
- 2 $Y_{20} - Y_{42}$
- 3 Six thousand three hundred seventy-one less than Z_1
- 4 Seventy-four times a prime number
- 5 Mean of X_{36} and X_1
- 6 Twice a prime number
- 7 Twice a prime number
- 8 $X_{29} \times X_{25}$
- 9 Last two digits are the same as last two digits of Y_{33}
- 10 $Y_{47} - Y_{37}$
- 11 A prime number
- 13 A prime number
- 14 Twice a prime number
- 15 Two thousand six hundred seventy-four more than Z_4
- 16 $X_{40} - Z_2$
- 17 A square
- 24 $X_{25} - X_8$
- 37 A square
- 41 Mean of Z_{24} and X_{26}
- 42 Mean of X_{35} and Z_{44}
- 44 $Y_{29} + X_{27}$

Solution:

3	2	2	1	3	5	8	9	5	2	7	■	3	6	4
2	2	■	2	3	2	0	5	9	7	6	4	8	4	5
6	5	6	4	7	8	1	■	3	■	■	4	■	3	6
8	1	2	5	4	4	8	■	6	0	3	2	■	■	0

3	2	6	1	1	3	5	2	4	2
■	2	■	8	4	1	■	■	4	2
5	2	6	2	■	3	7	5	1	9
8	8	7	9	■	6	8	■	8	6